

Exploiting Data to its Fullest

Machine Learning and Small Area Estimation

June 2023

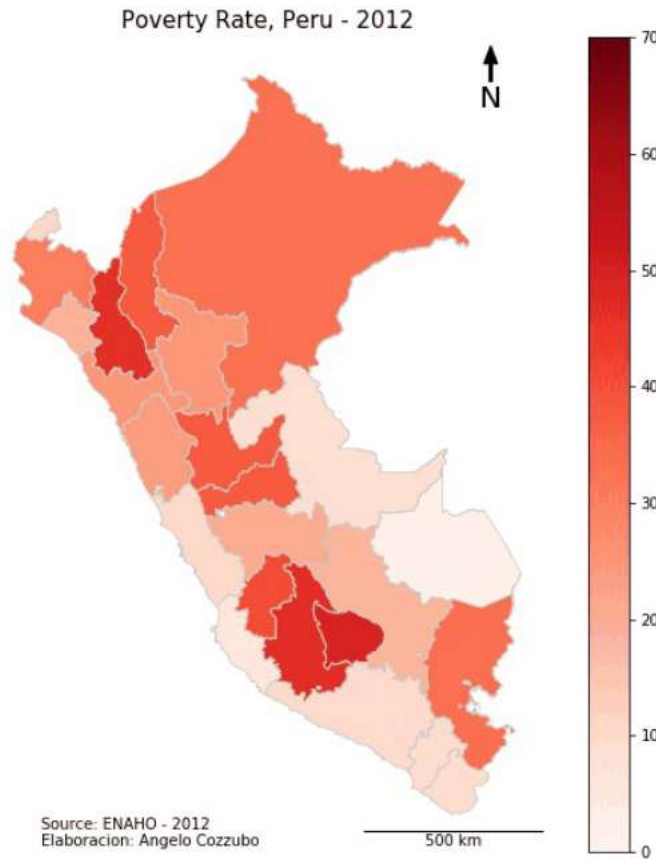
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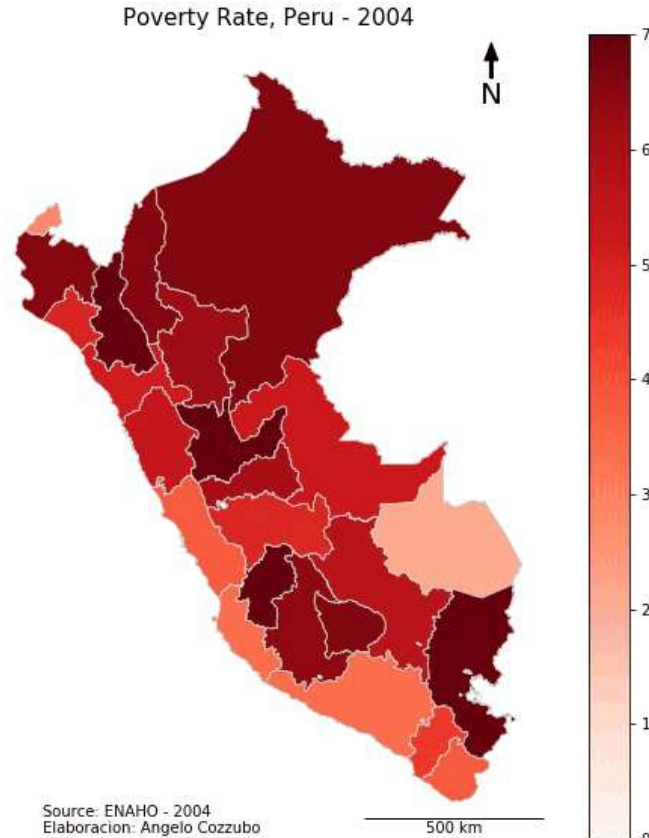


Exploiting Data to its Fullest

Traditional national surveys provide broad estimates

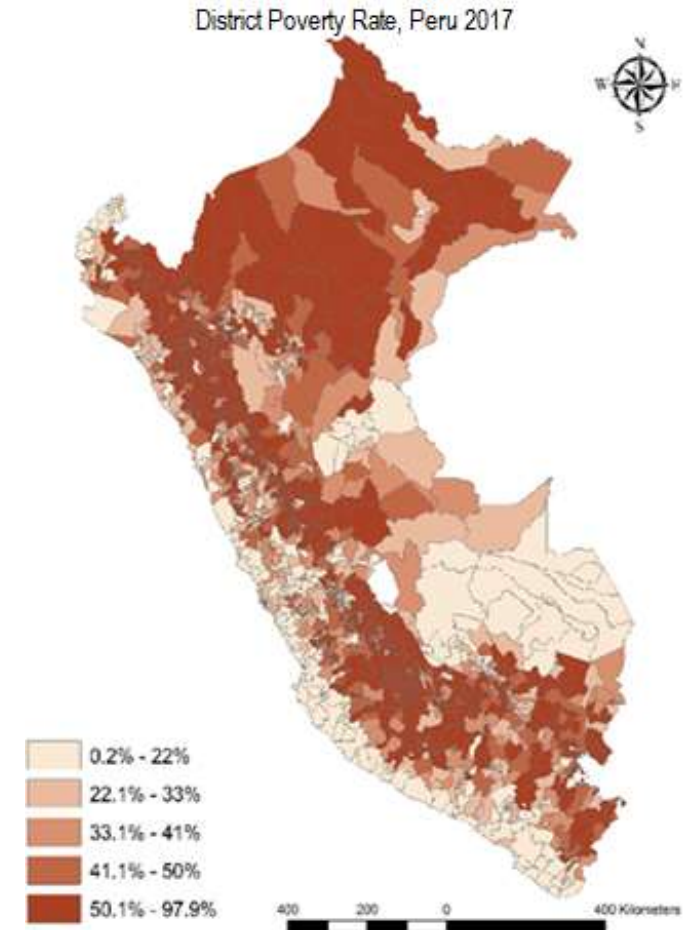


We may be lucky and even have many waves of data



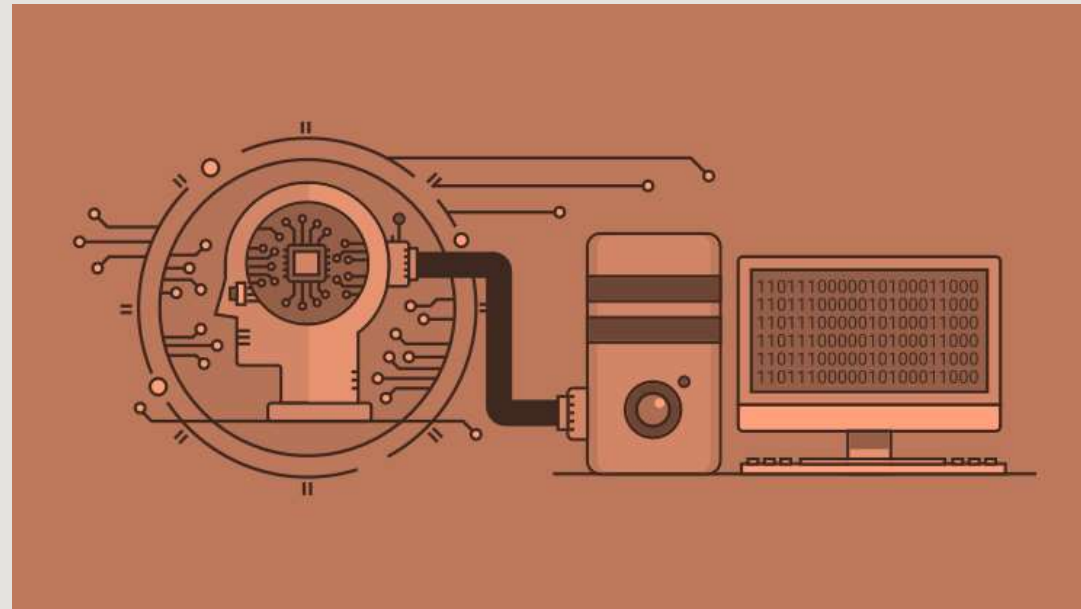
Why stop here?

We can use Small Area Estimation (SAE)



And again, why stop in traditional SAE?

Since SAE is a predictive task → potential to exploit Machine Learning

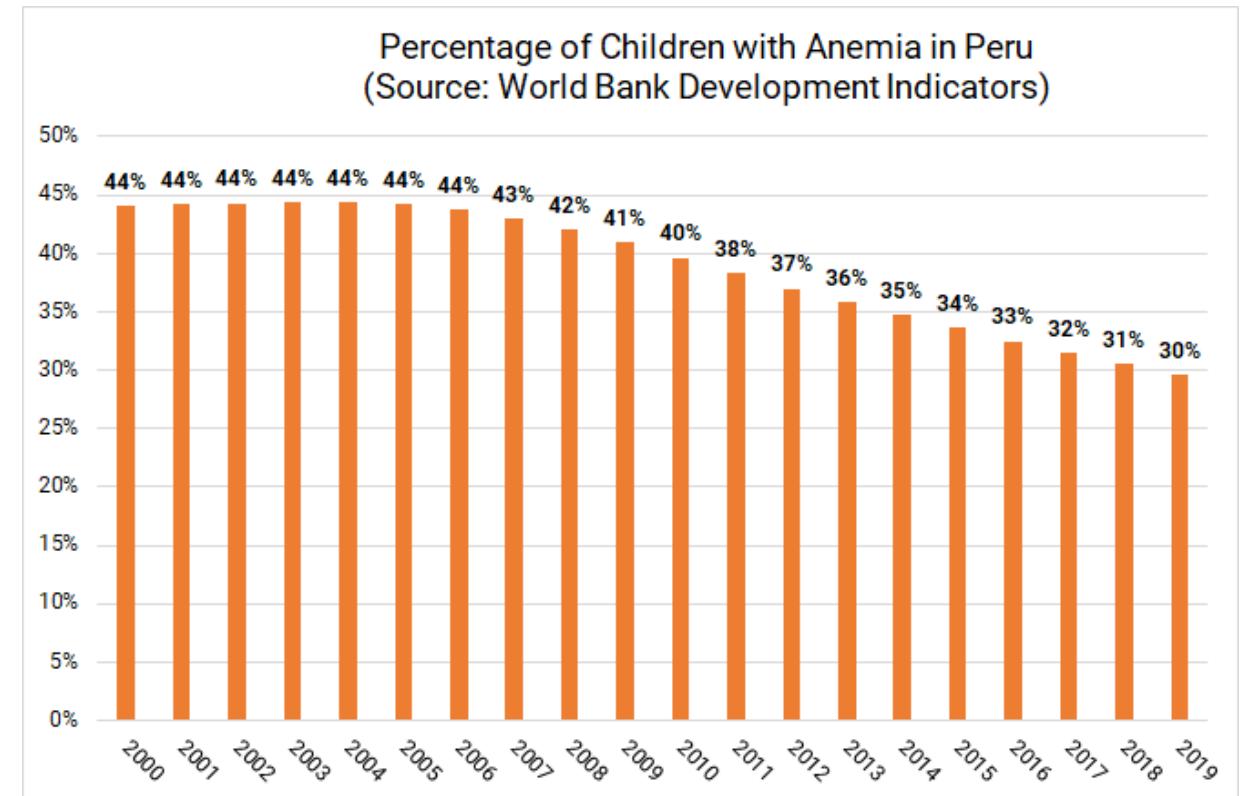


Our implementation

- ✓ SAE of anemia prevalence in Peru
- ✓ Pressing problem: local estimates not available
- ✓ Access to non-public rich datasets. **558 clean covariates**
- ✓ Special challenge: $K > N$
- ✓ Pool several waves of data

Anemia in Peru

- 2018 → National Plan to Combat Child Anemia
- Official estimates → Only at the regional level.
- Hard for policymakers to plan local interventions
- We built an anemia prevalence map
 - New SAE-ML approaches
 - Province-level estimates



Data Source: World Health Organization, Global Health Observatory Data Repository/World Health Statistics. Accessed via World Bank Development Indicators

Exploiting Data to its Fullest with Machine Learning

National Statistics Offices do not publish estimates with high uncertainty: UNRELIABLE

Objective → Reduce uncertainty of provincial-level estimates

- We used area level SAE models → Fay Herriot model
- Model *borrow strength* from administrative records and census covariates to reduce the uncertainty
- Spatial Fay Herriot: also borrows strength from neighbors
- We explore techniques to find the “best” set of covariates

- Expert's opinion



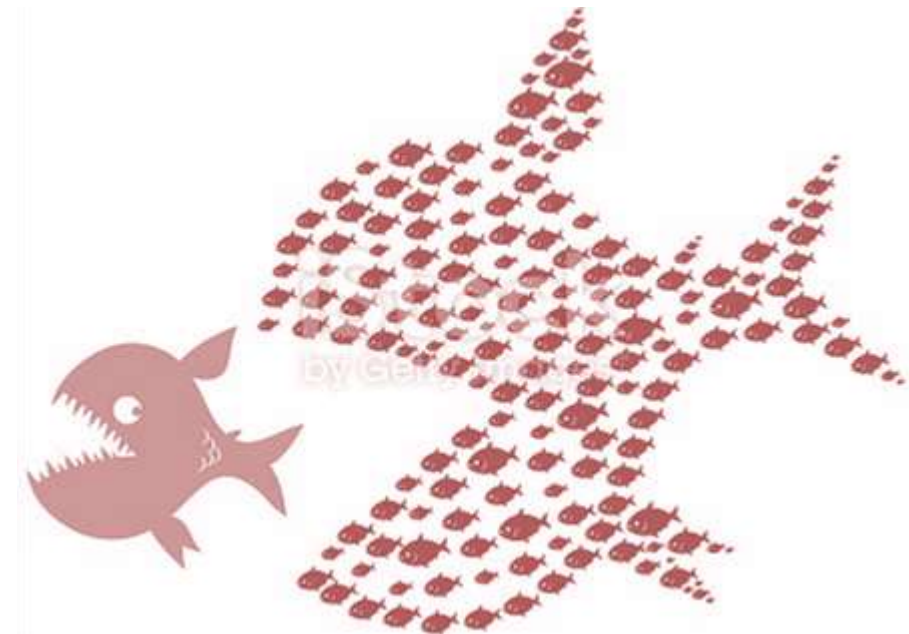
- Stepwise selection



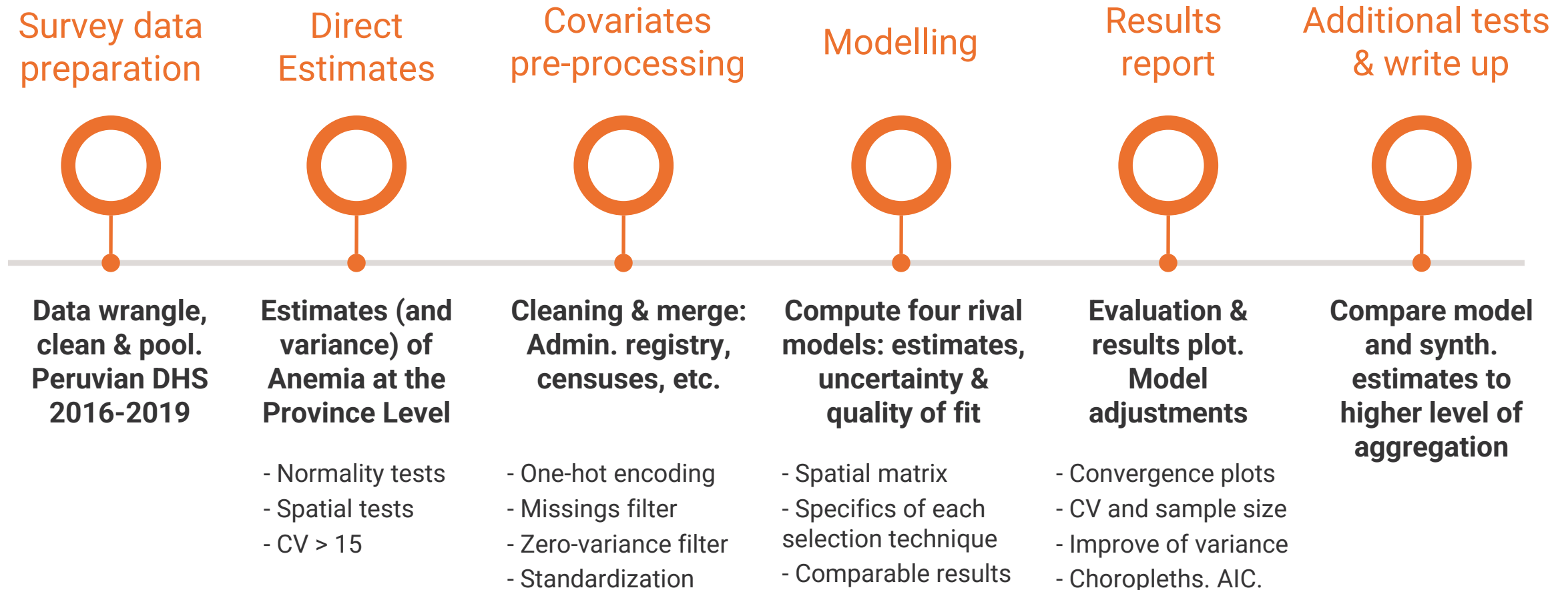
- LASSO



- Sparse PCA

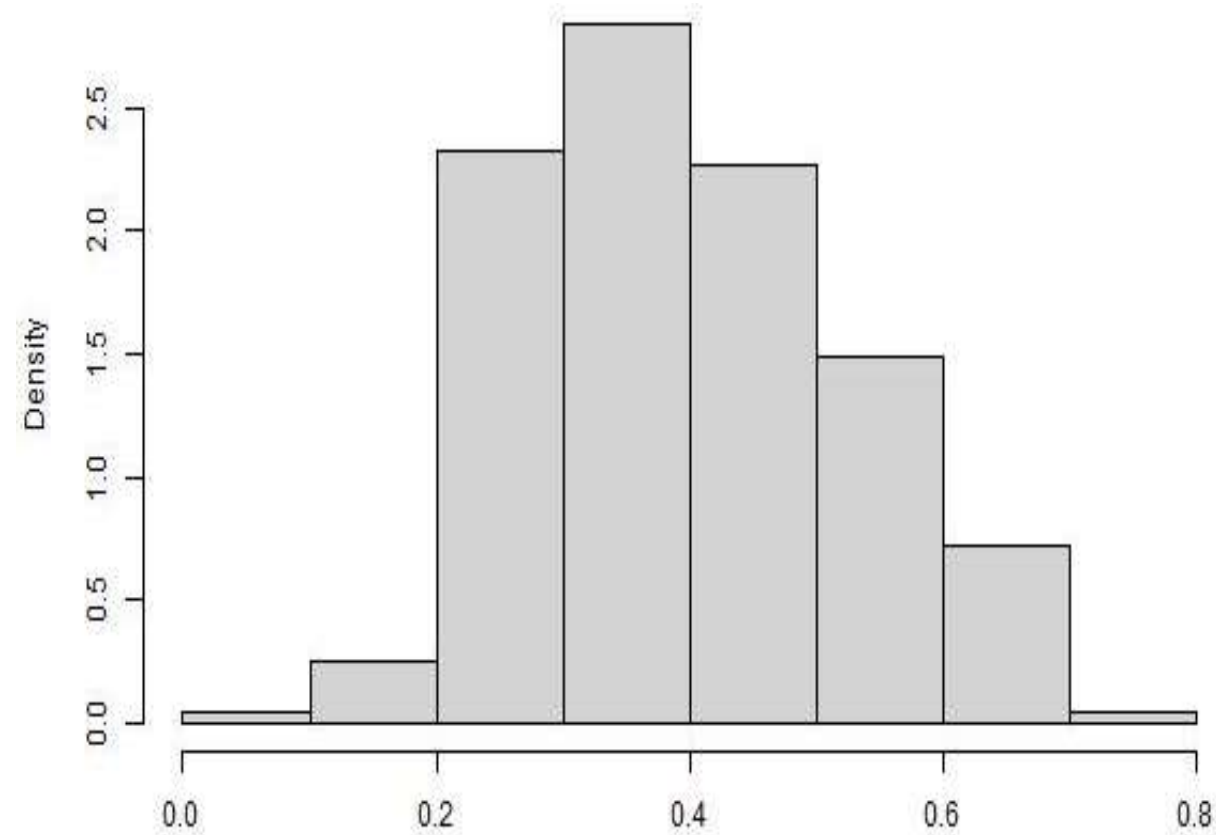


The process

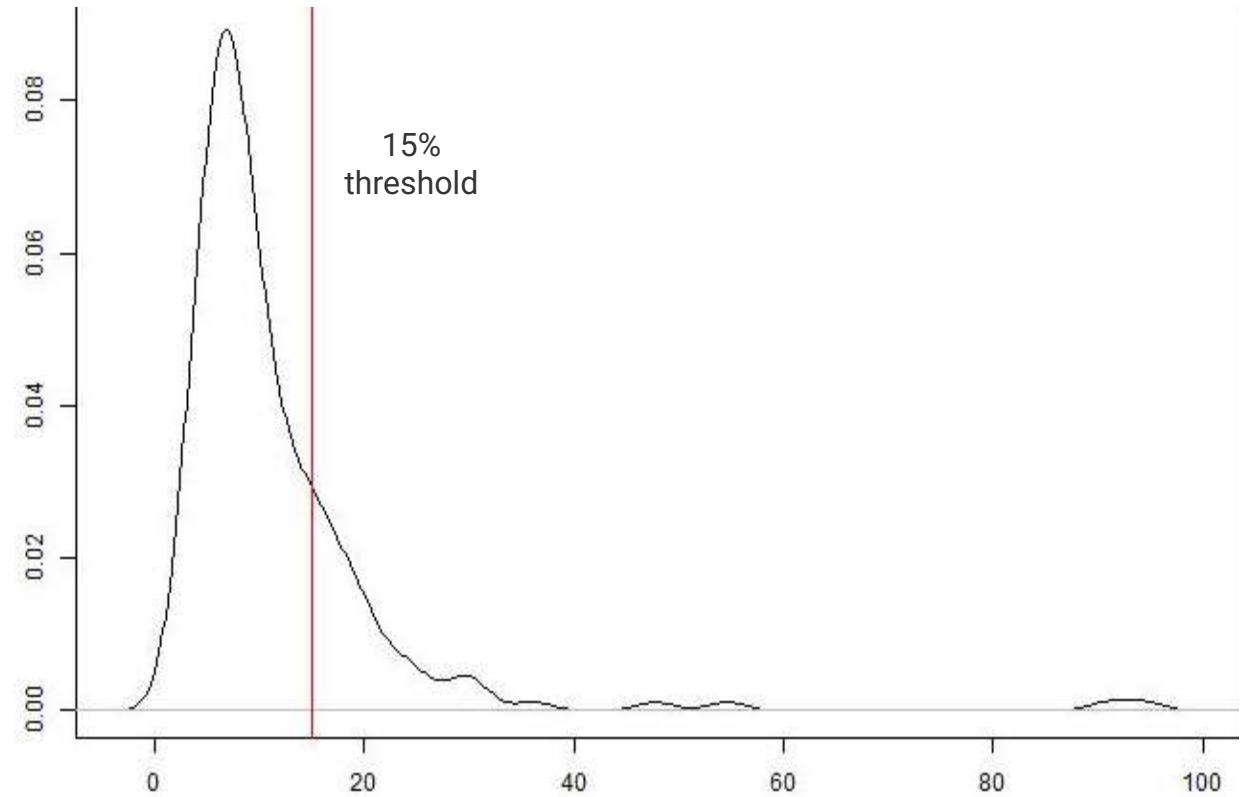


Anemia – 194 direct provincial estimates

Anemia Incidence



Coefficients of Variation



The (Spatial) Fay Herriot Model

Canonical area level model (1979). For a population characteristic θ_i (anemia)

$$\hat{Y}_i = \theta_i + e_i$$

$$\theta_i = x_i' \beta + u_i$$

- \hat{Y}_i : vector of direct HT estimates, $\forall i$ provinces
- e_i : vector sampling errors, independent of u_i
- x_i' : matrix of explanatory variables
- u_i : vector of area effects



Spatial extension. Borrows strength from neighbors

- u_i follows Spatial Autoregressive process

$$u_i = \rho W u_i + \eta_i$$

where ρ denoting the autoregression parameter, W a standardized queen proximity matrix and $\eta_i \sim N(0_i, A I_i)$ for A unknown

Rival models for covariate selection

Experts



Zoom interviews to Peruvian experts on health topics

Intersection criteria for the predictors

7 predictors

Stepwise



Bidirectional step method.

AIC and significance criteria

14 predictors

LASSO



Model with Random Effects

Hyperparameter by GridSearch. Correlation filter

97 predictors

Sparse PCA



PCA decomp. Selection main components

1-in-20 criteria. 80% of variance explained

10 predictors (components)

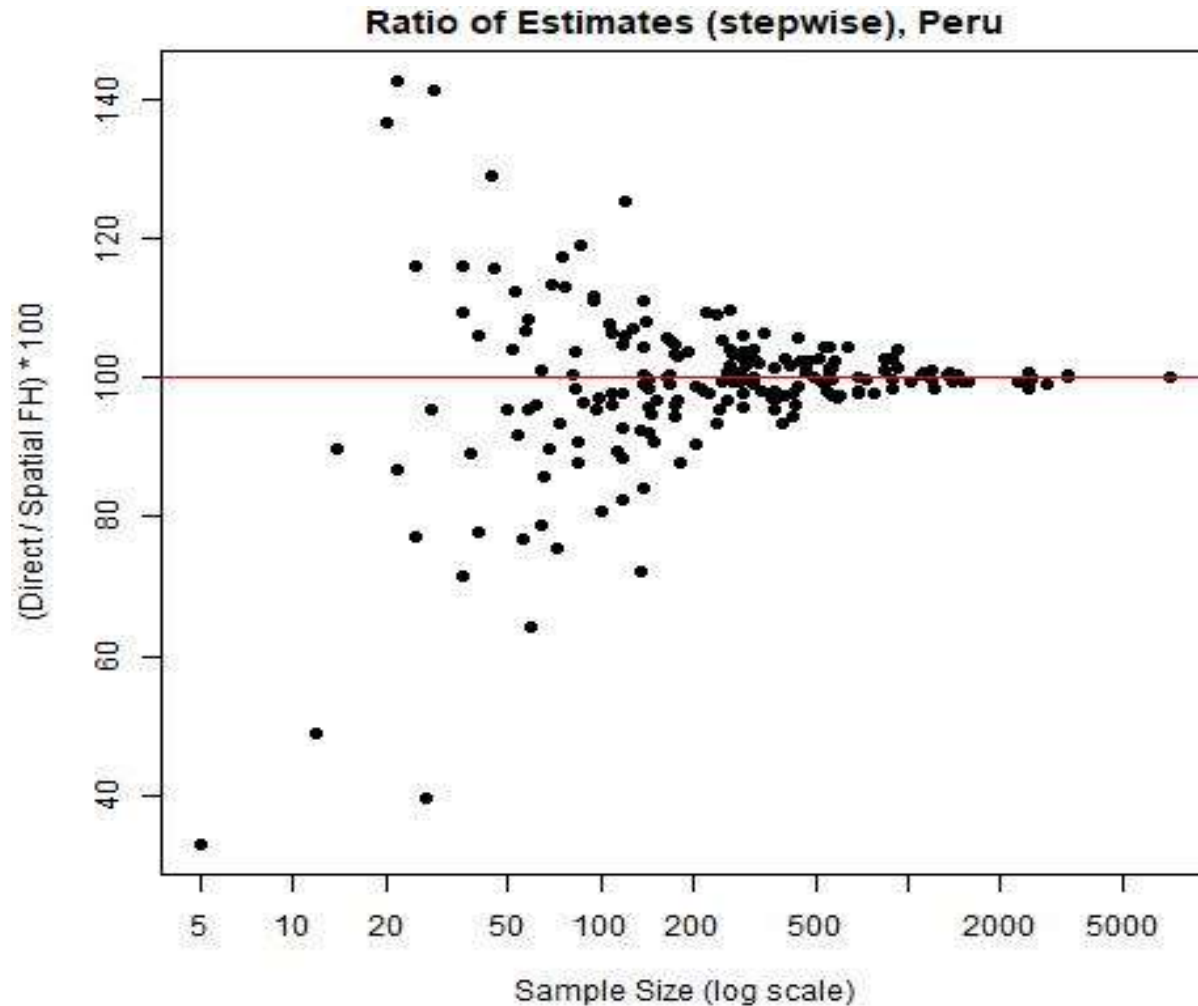


We computed Spatial Fay Herriot models

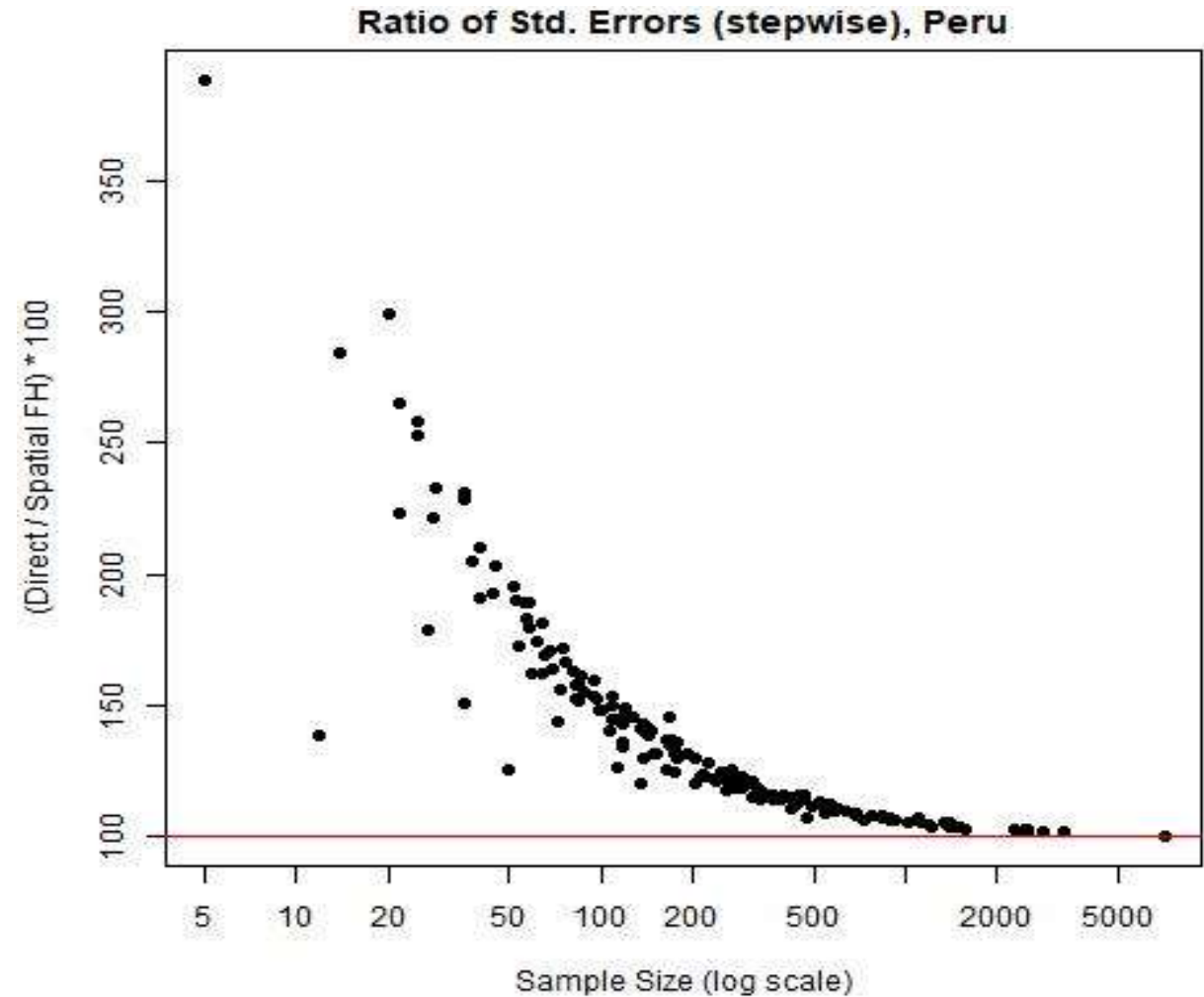
Use set of predictors chosen by each technique

Objective: Improve the variance of the province-level Anemia estimates

Results (I) – Convergence to direct estimate & reduction of variance



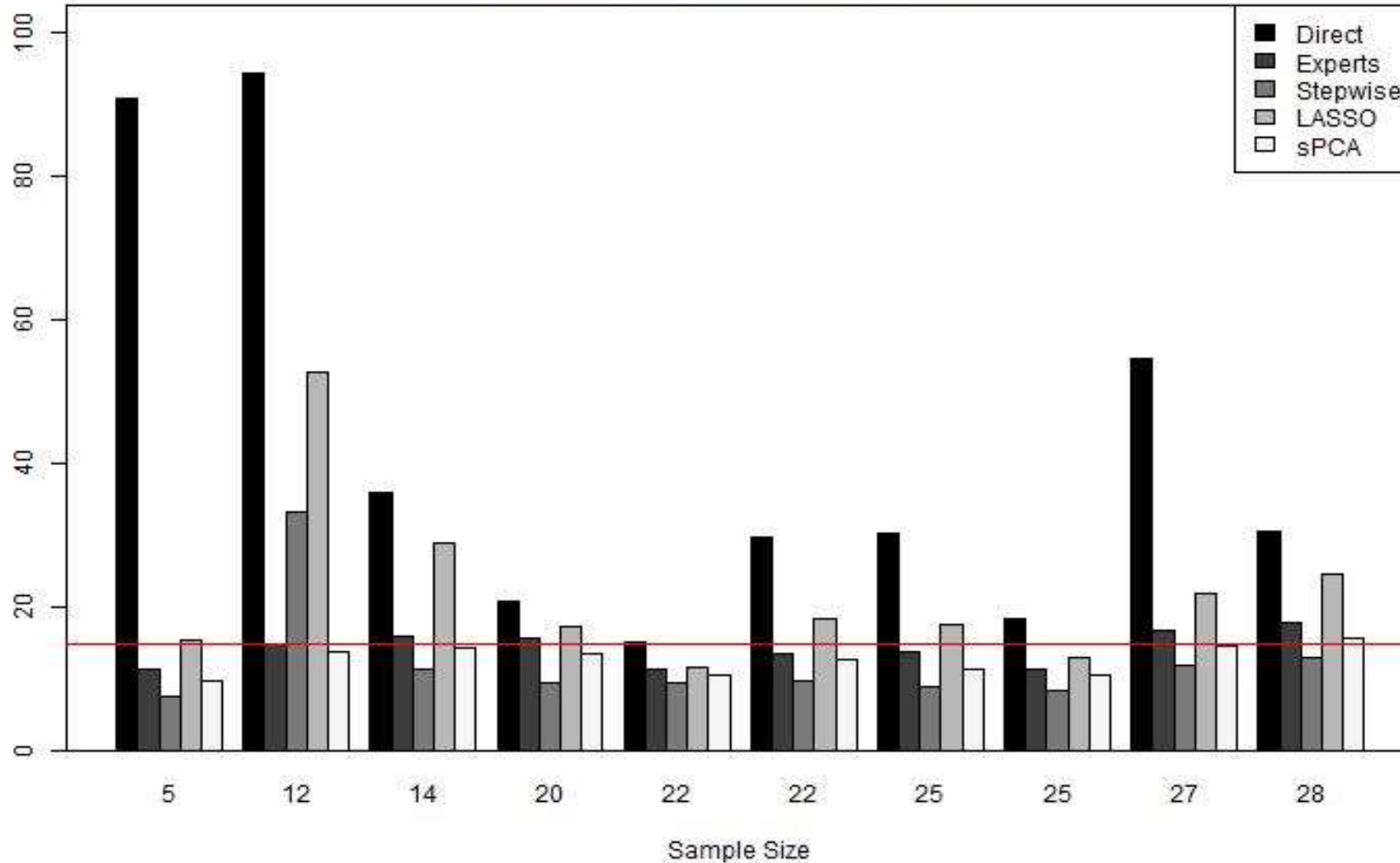
Note: FH = Fay-Harriot model, X-axis in logarithmic scale. Compiled by authors.



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Results (II) – All variable selection methods helped to reduce the CVs/variances. But some were more effective.

Coefficiente of Variation, provinces with smallest sample size



Median variance reduction percentage for each selection method:



Experts 24%



Stepwise 35%

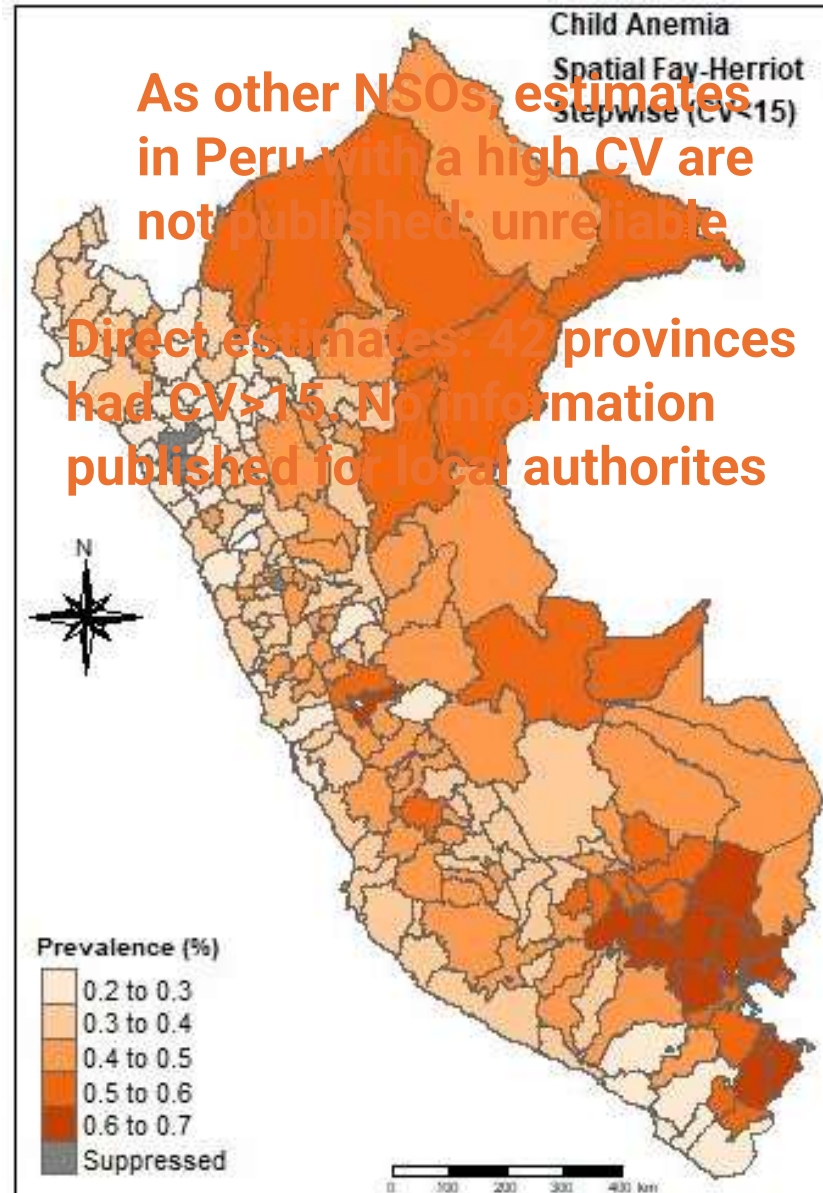
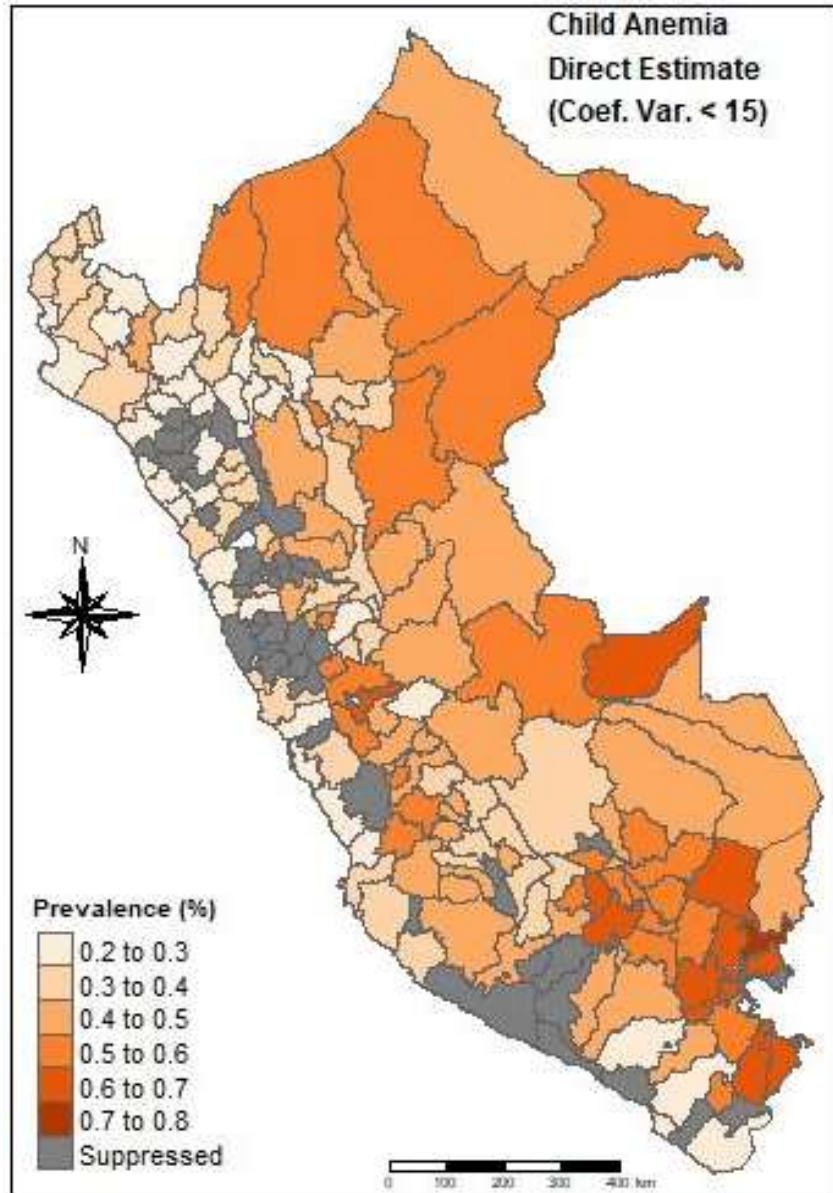


LASSO 12%



sPCA 28%

Results (III) – Recover estimates for 20% of the provinces



By SAE methods, suppressed estimates are reduced to



Experts 13

Stepwise 3



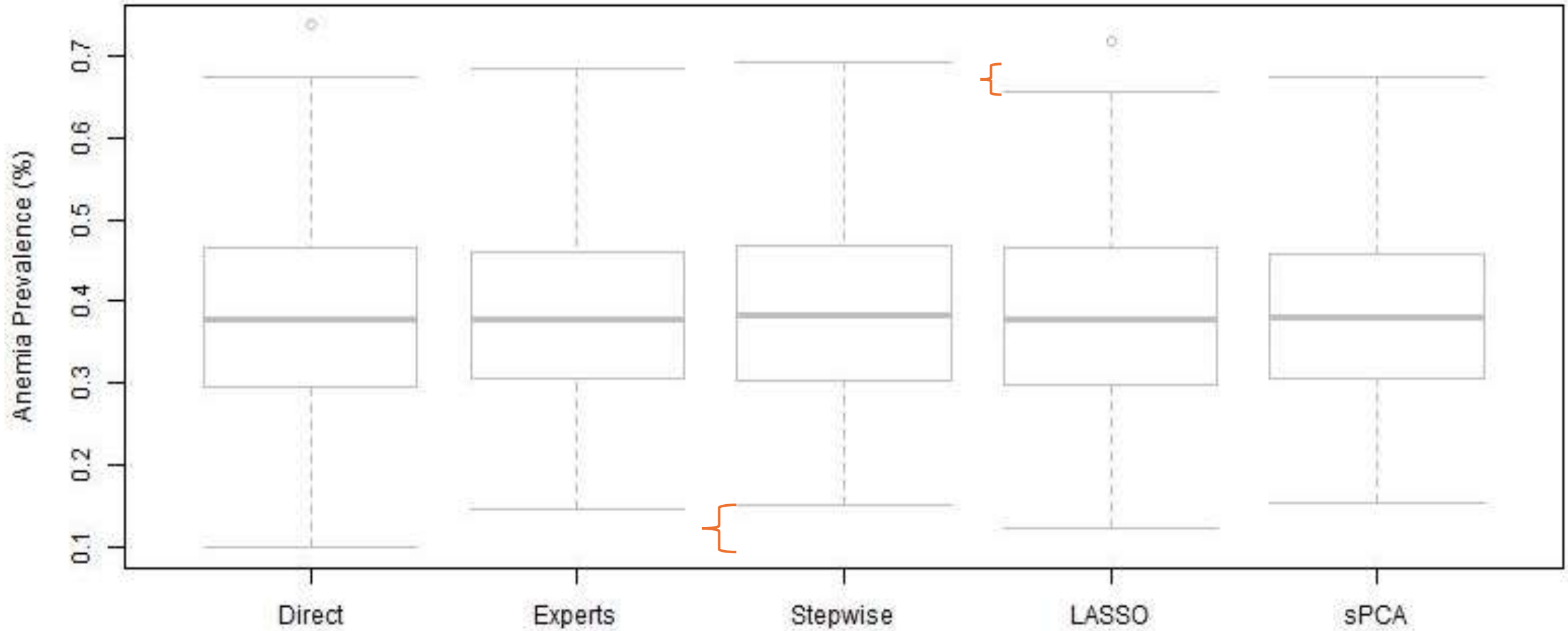
LASSO 25



sPCA 5



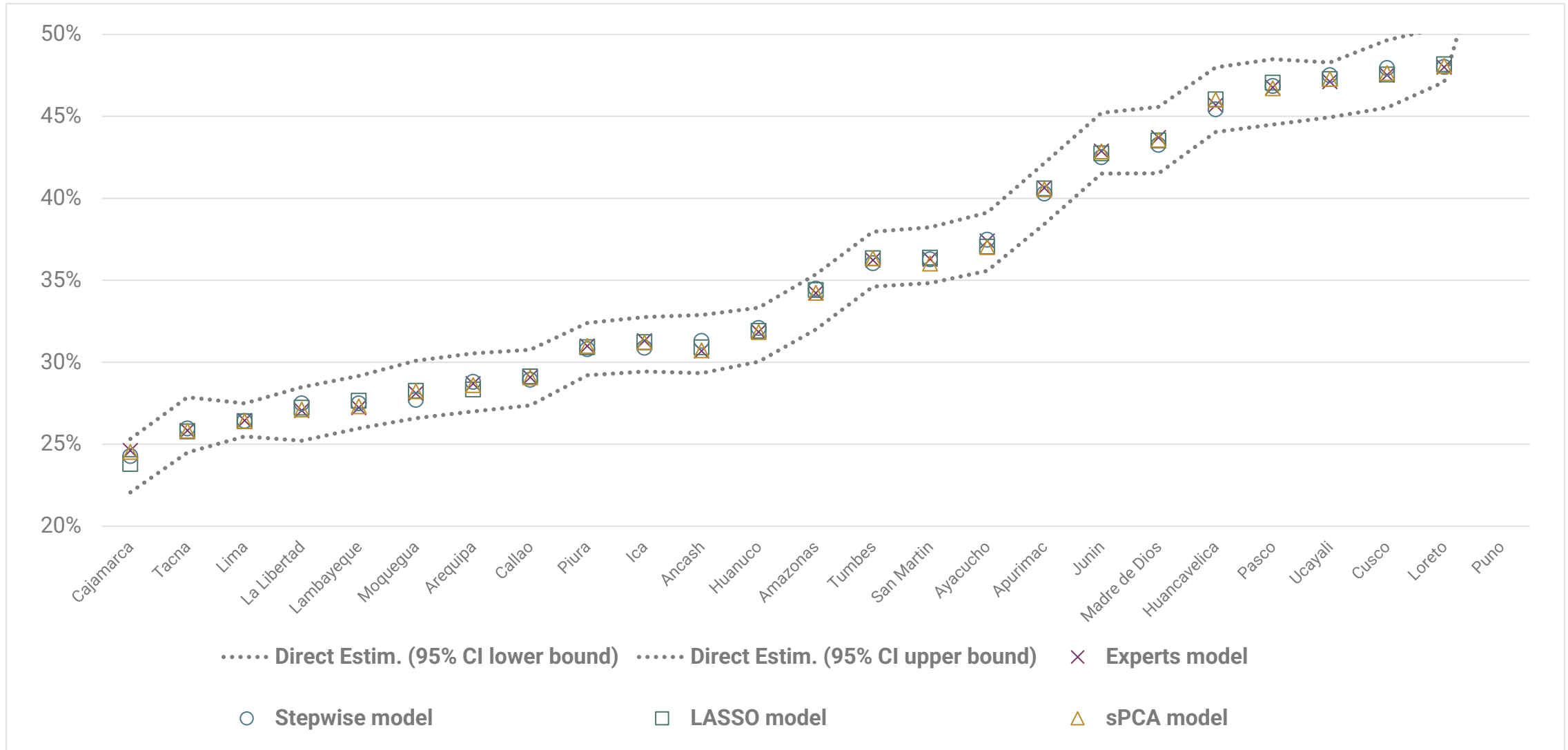
Additional tests – Estimates comparison



Additional tests – Quality of fit

Model	Log Likelihood	AIC	BIC
Experts	201.6	-385.3	-355.9
Stepwise	273.7	-513.3	-457.8
LASSO	280.1	-360.3	-33.5
Sparse PCA	221.8	-417.7	-375.2

Additional tests – Model estimates (\hat{Y}_i^{FH}) at the region level



Additional tests – Synthetic estimates ($x_i' \hat{\beta}$) at the region level

Remember the FH model

$$\begin{aligned}\hat{Y}_i &= \theta_i + e_i \\ \theta_i &= x_i' \beta + u_i\end{aligned}$$

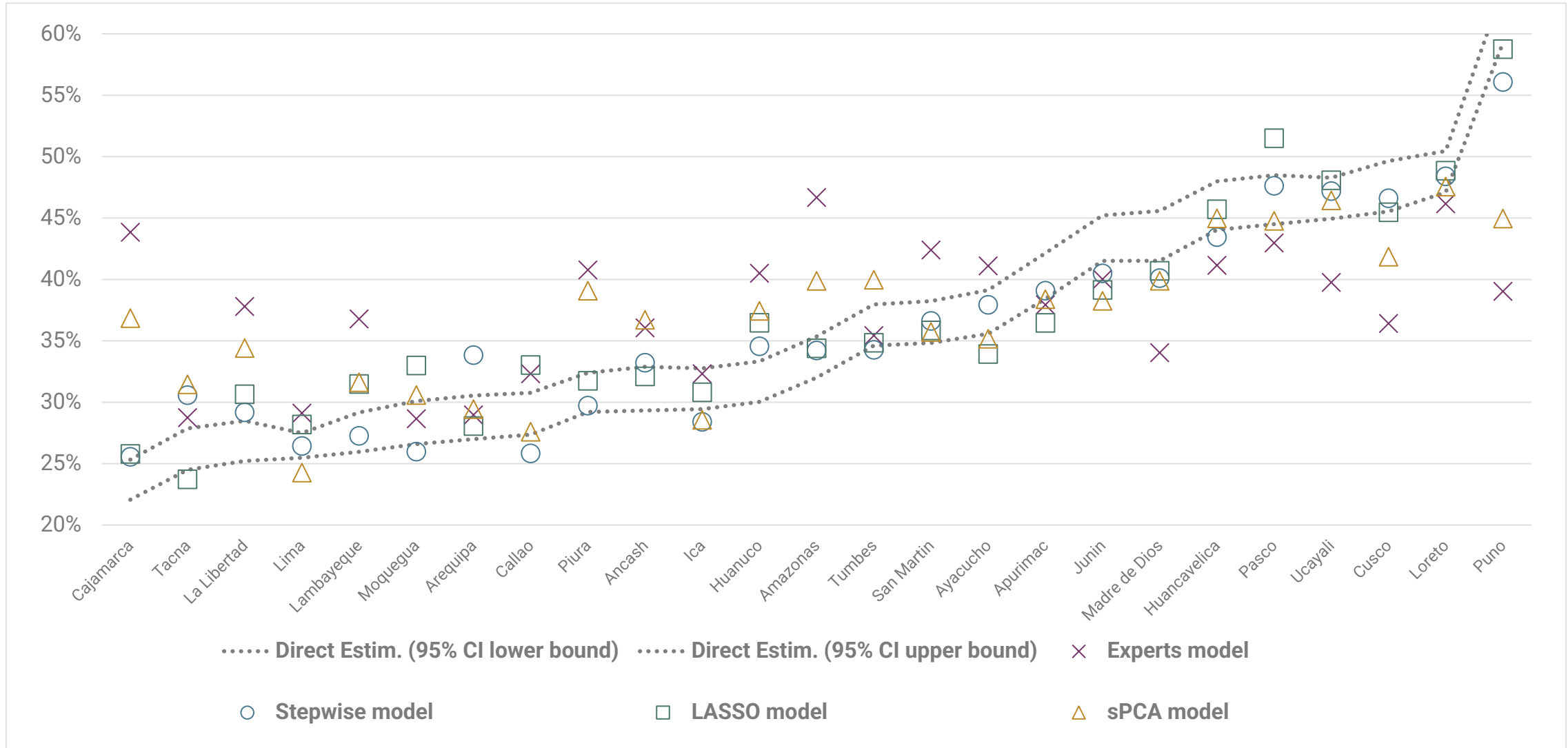
And the best linear predictor of θ_i

$$\hat{\theta}_i = (1 - \gamma_i) \hat{Y}_i + \gamma_i x_i' \hat{\beta}$$

Then, FH estimator is a weighted linear combination of

- Direct estimator: \hat{Y}_i
- Synthetic estimator: $x_i' \hat{\beta}$

Additional tests – Synthetic estimates ($x'_p \hat{\beta}$) at the region level



Results by the Numbers

39 out of 42

**Suppressed provincial
estimates were recovered**

~33,000

**Anemic children in
recovered provinces**

35%

**Median variance
reduction**

Takeaways

SAE modelling to reduce uncertainty of local estimates

We studied alternative methods for covariate selection from a large pool of candidates (+500)

Stepwise model outperformed other methods based on our metrics

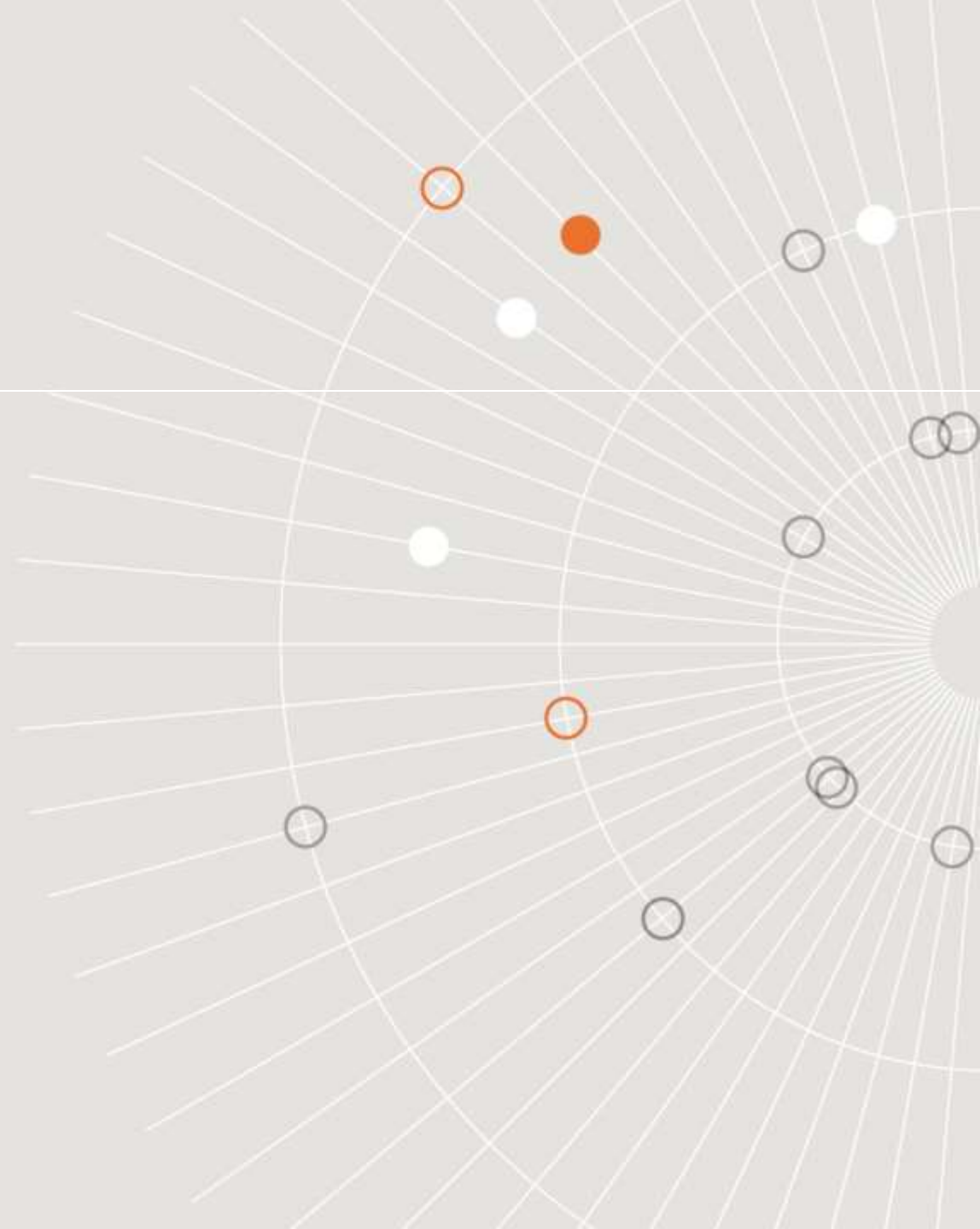


Borrow strength from administrative records, censuses, and neighbors' data

We applied our models to the child anemia problem in Peru. Great uncertainty reduction

Tackled an unresolved statistical problem in Peru. Opportunity for other health applications.

Questions?



Thank you.

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 Research You Can Trust™



Appendix

Variables selected by the Stepwise method

From Administrative Records

- Total children under 3 years with anemia
Percentage 2018
- Children under 3 years with severe anemia
Percentage 2018
- Children under 5 years with mild anemia
Percentage 2018
- Children under 5 years with severe anemia
Percentage 2018
- Percentage of students in public school who only achieved undemanding tasks
- Percentage of students in a private school who achieved a partial learning objectives

From Population Census

- Household does not use manure for cooking
- House walls made of adobe or quincha
- Household does not have a refrigerator or freezer
- Household has a gas stove
- Household has a cell phone
- Household does not have a sound system
- Household has a motorcycle
- Household does not have an electric iron